

6)

\mathbb{R}^3	$\overset{\checkmark}{l_1} (1, 1, 0)$ $\overset{w}{l_2} (1, 0, 1)$	$(0, 1, -1) \overset{w}{l_3}$ $(3, 1, 2) \overset{w}{l_5}$	z	z	z	z
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V/W: $a l_1 + b l_2 = c l_3 + d l_5 \leadsto$

$\leadsto a l_1 + b l_2 - c l_3 - d l_5 = 0$

$$\begin{pmatrix} \overset{l_1}{1} & \overset{l_2}{1} & \overset{l_3}{0} & \overset{l_5}{3} \\ 1 & 0 & 1 & 1 \\ 0 & 1 & -1 & 2 \end{pmatrix} \begin{pmatrix} a \\ b \\ -c \\ -d \end{pmatrix} = 0$$

$$\begin{pmatrix} \overset{l_1}{1} & \overset{l_2}{1} & \overset{l_3}{0} & \overset{l_5}{3} \\ 1 & 0 & 1 & 1 \\ 0 & 1 & -1 & 2 \end{pmatrix} \leadsto \begin{pmatrix} 1 & 1 & 0 & 3 \\ 0 & -1 & 1 & -2 \\ 0 & 0 & 0 & 0 \end{pmatrix} \leadsto \begin{cases} a + b - 3d = 0 \\ -b - c + 2d = 0 \end{cases}$$

$$\leadsto \begin{cases} a = -b + 3d = c + d \\ b = -c + 2d \end{cases} \quad \begin{cases} a = s + \delta \\ b = -s + 2\delta \\ c = s \\ d = \delta \end{cases}$$

VERIFICA:

$$\leadsto (s + \delta) \overset{l_1}{\begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}} + (-s + 2\delta) \overset{l_2}{\begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}} = s \begin{pmatrix} 1-1 \\ 1-0 \\ 0-1 \end{pmatrix} + \delta \begin{pmatrix} 1+2 \\ 1+0 \\ 0+2 \end{pmatrix} =$$

$$= s \overset{l_3}{\begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}} + \delta \overset{l_5}{\begin{pmatrix} 3 \\ 1 \\ 2 \end{pmatrix}}$$

$\leadsto V/W = \text{SPAN} \{ l_1, l_2 \} = \text{SPAN} \{ l_3, l_5 \}$